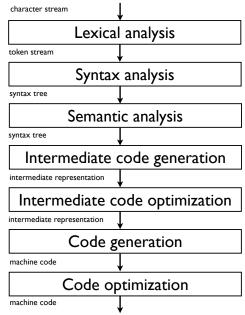
# Part 3 Syntax analysis

### Outline

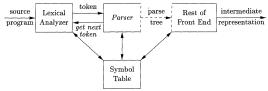
### 1. Introduction

- 2. Context-free grammar
- 3. Top-down parsing
- 4. Bottom-up parsing
- 5. Conclusion and some practical considerations

# Structure of a compiler



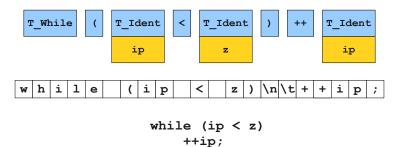
# Syntax analysis



### Goals:

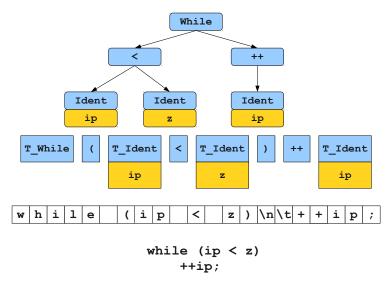
- recombine the tokens provided by the lexical analysis into a structure (called *a syntax tree*)
- Reject invalid texts by reporting syntax errors.
- Like lexical analysis, syntax analysis is based on
  - the definition of valid programs based on some formal languages,
  - the derivation of an algorithm to detect valid words (programs) from this language
- Formal language: context-free grammars
- Two main algorithm families: Top-down parsing and Bottom-up parsing

Example



(Keith Schwarz)

### Example



(Keith Schwarz)

### Reminder: grammar

- A grammar is a 4-tuple  $G = (V, \Sigma, R, S)$ , where:
  - V is an alphabet,
  - Σ ⊆ V is the set of terminal symbols (V − Σ is the set of nonterminal symbols),
  - $R \subseteq (V^+ \times V^*)$  is a finite set of production rules
  - $S \in V \Sigma$  is the start symbol.
- Notations:
  - ▶ Nonterminal symbols are represented by uppercase letters: A,B,...
  - ► Terminal symbols are represented by lowercase letters: *a*,*b*,...
  - Start symbol written as S
  - Empty word: e
  - A rule  $(\alpha, \beta) \in R : \alpha \to \beta$
  - Rule combination:  $A \rightarrow \alpha | \beta$
- Example:  $\Sigma = \{a, b, c\}, V \Sigma = \{S, R\}, R =$

$$egin{array}{cccc} S & 
ightarrow & R \ S & 
ightarrow & aSc \ R & 
ightarrow & \epsilon \ R & 
ightarrow & RbR \end{array}$$

### Reminder: derivation and language

Definitions:

- v can be *derived in one step* from u by G (noted  $v \Rightarrow u$ ) iff u = xu'y, v = xv'y, and  $u' \rightarrow v'$
- v can be *derived in several steps* from u by G (noted  $v \stackrel{*}{\Rightarrow} u$ ) iff  $\exists k \ge 0$  and  $v_0 \ldots v_k \in V^+$  such that  $u = v_0, v = v_k, v_i \Rightarrow v_{i+1}$  for  $0 \le i < k$
- The *language generated by a grammar G* is the set of words that can be derived from the start symbol:

$$L = \{w \in \Sigma^* | S \stackrel{*}{\Rightarrow} w\}$$

Example: derivation of *aabcc* from the previous grammar

$$\underline{S} \Rightarrow a\underline{S}c \Rightarrow aa\underline{S}cc \Rightarrow aa\underline{R}cc \Rightarrow aa\underline{R}bRcc \Rightarrow aab\underline{R}cc \Rightarrow aabcc$$

# Reminder: type of grammars

Chomsky's grammar hierarchy:

- Type 0: free or unrestricted grammars
- Type 1: context sensitive grammars
  - ▶ productions of the form  $uXw \rightarrow uvw$ , where u, v, w are arbitrary strings of symbols in V, with v non-null, and X a single nonterminal
- Type 2: context-free grammars (CFG)
  - ▶ productions of the form X → v where v is an arbitrary string of symbols in V, and X a single nonterminal.
- Type 3: regular grammars
  - Productions of the form X → a, X → aY or X → e where X and Y are nonterminals and a is a terminal (equivalent to regular expressions and finite state automata)

### Context-free grammars

- Regular languages are too limited for representing programming languages.
- Examples of languages not representable by a regular expression:
  - $L = \{a^n b^n | n \ge 0\}$
  - ▶ Balanced parentheses L = {€, (), (()), ()(), ((())), (())()...}
  - Scheme programs
    - $L = \{1, 2, 3, \dots, (lambda(x)(+x1))\}$
- Context-free grammars are typically used for describing programming language syntaxes.
  - They are sufficient for most languages
  - They lead to efficient parsing algorithms

# Context-free grammars for programming languages

- Nonterminals of the grammars are typically the tokens derived by the lexical analysis (in bold in rules)
- Divide the language into several syntactic categories (sub-languages)
- Common syntactic categories
  - Expressions: calculation of values
  - Statements: express actions that occur in a particular sequence
  - Declarations: express properties of names used in other parts of the program
  - $Exp \rightarrow Exp + Exp$
  - $Exp \rightarrow Exp Exp$
  - $Exp \rightarrow Exp * Exp$
  - $Exp \rightarrow Exp/Exp$
  - $Exp \rightarrow num$

 $Exp \rightarrow (Exp)$ 

 $Exp \rightarrow id$ 

- Stat  $\rightarrow$  id := Exp
- $\textit{Stat} \ \rightarrow \ \textit{Stat}; \textit{Stat}$
- Stat  $\rightarrow$  if Exp then Stat Else Stat
- Stat  $\rightarrow$  if Exp then Stat

### Derivation for context-free grammar

- Like for a general grammar
- Because there is only one nonterminal in the LHS of each rule, their order of application does not matter
- Two particular derivations
  - left-most: always expand first the left-most nonterminal (important for parsing)
  - right-most: always expand first the right-most nonterminal (canonical derivation)

Examples

 $egin{array}{rcl} S & 
ightarrow & aTb|c \ T & 
ightarrow & cSS|S \end{array}$ 

w = accacbb

Left-most derivation:  $S \Rightarrow aTb \Rightarrow acSSb \Rightarrow accSb \Rightarrow$  $accaTbb \Rightarrow accaSbb \Rightarrow accacbb$ 

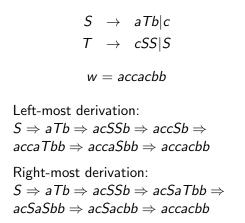
Right-most derivation:  $S \Rightarrow aTb \Rightarrow acSSb \Rightarrow acSaTbb \Rightarrow$  $acSaSbb \Rightarrow acSacbb \Rightarrow accacbb$ 

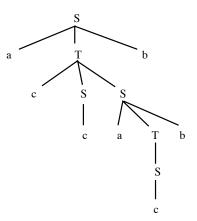
### Parse tree

A parse tree abstracts the order of application of the rules

- Each interior node represents the application of a production
- For a rule A → X<sub>1</sub>X<sub>2</sub>...X<sub>k</sub>, the interior node is labeled by A and the children from left to right by X<sub>1</sub>, X<sub>2</sub>,...,X<sub>k</sub>.
- Leaves are labeled by nonterminals or terminals and read from left to right represent a string generated by the grammar
- A derivation encodes how to produce the input
- A parse tree encodes the structure of the input
- Syntax analysis = recovering the parse tree from the tokens

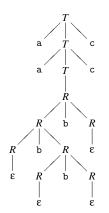
### Parse trees

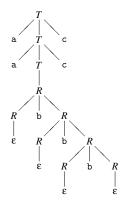




Parse tree



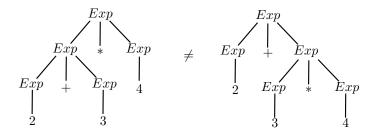




Syntax analysis

# Ambiguity

- The order of derivation does not matter but the chosen production rules do
- Definition: A CFG is ambiguous if there is at least one string with two or more parse trees
- Ambiguity is not problematic when dealing with flat strings. It is when dealing with language semantics



# Detecting and solving Ambiguity

- There is no mechanical way to determine if a grammar is (un)ambiguous (this is an undecidable problem)
- In most practical cases however, it is easy to detect and prove ambiguity.

E.g., any grammar containing  $N \rightarrow N\alpha N$  is ambiguous (two parse trees for  $N\alpha N\alpha N$ ).

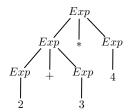
- How to deal with ambiguities?
  - Modify the grammar to make it unambiguous
  - Handle these ambiguities in the parsing algorithm
- Two common sources of ambiguity in programming languages
  - Expression syntax (operator precedences)
  - Dangling else

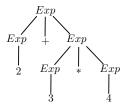
### Operator precedence

This expression grammar is ambiguous

(it contains  $N \rightarrow N \alpha N$ )

• Parsing of 2 + 3 \* 4





### Operator associativity

- Types of operator associativity:
  - An operator ⊕ is left-associative if a ⊕ b ⊕ c must be evaluated from left to right, i.e., as (a ⊕ b) ⊕ c
  - An operator ⊕ is right-associative if a ⊕ b ⊕ c must be evaluated from right to left, i.e., as a ⊕ (b ⊕ c)
  - An operator  $\oplus$  is non-associative if expressions of the form  $a \oplus b \oplus c$  are not allowed
- Examples:
  - $\blacktriangleright$  and / are typically left-associative
  - + and \* are mathematically associative (left or right). By convention, we take them left-associative as well
  - List construction in functional languages is right-associative
  - Arrows operator in C is right-associative (a->b->c is equivalent to a->(b->c))
  - In Pascal, comparison operators are non-associative (you can not write 2 < 3 < 4)</li>

### Rewriting ambiguous expression grammars

• Let's consider the following ambiguous grammar:

 $\begin{array}{rcl} E & \rightarrow & E \oplus E \\ E & \rightarrow & \operatorname{num} \end{array}$ 

■ If ⊕ is left-associative, we rewrite it as a left-recursive (a recursive reference only to the left). If ⊕ is right-associative, we rewrite it as a right-recursive (a recursive reference only to the right).

 $\oplus$  left-associative  $\oplus$  right-associative

Mixing operators of different precedence levels

Introduce a different nonterminal for each precedence level

#### Non-ambiguous

Ambiguous		Exp	$\rightarrow$	Exp + Exp2	Parse tree for $2 + 3$
		-			Exp
Exp $\rightarrow$	Exp + Exp	Exp	$\rightarrow$	Exp – Exp2	
Exp $ ightarrow$	Exp – Exp	Exp	$\rightarrow$	Exp2	Exp + $Exp2$
$\textit{Exp} \rightarrow$	Exp * Exp	Exp2	$\rightarrow$	Exp2 * Exp3	
$Exp \rightarrow$	Exp/Exp	Exp2	$\rightarrow$	Exp2/Exp3	Exp2 Exp2 *
$Exp \rightarrow$	num	Exp2	$\rightarrow$	Exp3	Exp3 Exp3
Exp $ ightarrow$	(Exp)	Exp3	$\rightarrow$	num	
		Exp3	$\rightarrow$	(Exp)	2 3

\* 4

Exp3

### Dangling else

Else part of a condition is typically optional

 $\begin{array}{rcl} \textit{Stat} & \rightarrow & \textit{if } \textit{Exp then } \textit{Stat Else } \textit{Stat} \\ \textit{Stat} & \rightarrow & \textit{if } \textit{Exp then } \textit{Stat} \end{array}$ 

- How to match if p then if q then s1 else s2?
- Convention: else matches the closest not previously matched if.
- Unambiguous grammar:

Stat —	Y	Matched Unmatched
Matched —	Y	if Exp then Matched else Matched
Matched —	Y	"Any other statement"
Unmatched —	>	if Exp then Stat
Unmatched —	Y	if Exp then Matched else Unmatched

### End-of-file marker

- Parsers must read not only terminal symbols such as +,-, num , but also the end-of-file
- We typically use \$ to represent end of file
- If S is the start symbol of the grammar, then a new start symbol S' is added with the following rules  $S' \rightarrow S$ .

S	$\rightarrow$	Exp\$
Exp	$\rightarrow$	Exp + Exp2
Exp	$\rightarrow$	Exp – Exp2
Exp	$\rightarrow$	Exp2
Exp2	$\rightarrow$	Exp2 * Exp3
Exp2	$\rightarrow$	Exp2/Exp3
Exp2	$\rightarrow$	Exp3
Exp3	$\rightarrow$	num
<b>F</b>		( [

### Non-context free languages

- Some syntactic constructs from typical programming languages cannot be specified with CFG
- Example 1: ensuring that a variable is declared before its use
  - $L_1 = \{wcw | w \text{ is in } (a|b)^*\}$  is not context-free
  - In C and Java, there is one token for all identifiers
- Example 2: checking that a function is called with the right number of arguments
  - $L_2 = \{a^n b^m c^n d^m | n \ge 1 \text{ and } m \ge 1\}$  is not context-free
  - In C, the grammar does not count the number of function arguments

$$stmt \rightarrow id (expr_list)$$
  
 $expr_list \rightarrow expr_list, expr$   
 $| expr$ 

These constructs are typically dealt with during semantic analysis

### Backus-Naur Form

- A text format for describing context-free languages
- We ask you to provide the source grammar for your project in this format
- Example:

<pre><expression></expression></pre>	::= <term>   <term> "+" <expression></expression></term></term>
<term></term>	::= <factor> <factor> "*" <term></term></factor></factor>
<factor></factor>	::= <constant>   <variable>   "(" <expression> ")"</expression></variable></constant>
<variable></variable>	::= "x"   "y"   "z"
<constant></constant>	::= <digit>   <digit> <constant></constant></digit></digit>
<digit></digit>	::= "0"   "1"   "2"   "3"   "4"   "5"   "6"   "7"   "8"   "9"

More information: http://en.wikipedia.org/wiki/Backus-Naur\_form

### Outline

### 1. Introduction

- 2. Context-free grammar
- 3. Top-down parsing
- 4. Bottom-up parsing
- 5. Conclusion and some practical considerations

### Syntax analysis

### Goals:

- Checking that a program is accepted by the context-free grammar
- Building the parse tree
- Reporting syntax errors
- Two ways:
  - Top-down: from the start symbol to the word
  - Bottom-up: from the word to the start symbol

# Top-down and bottom-up: example

Grammar:

$$\begin{array}{cccc} S & 
ightarrow & AB \ A & 
ightarrow & aA|\epsilon \ B & 
ightarrow & b|bB \end{array}$$

Top-down <i>S</i>	parsing of <i>aaab</i>
AB	S  ightarrow AB
aAB	A  ightarrow a $A$
aaAB	A  ightarrow aA
aaaAB	A  ightarrow aA
aaa $\epsilon B$	$A  ightarrow \epsilon$
aaab	B  ightarrow b

Bottom-ı	up parsing of <i>aaab</i>
aaau	
aaa $\epsilon$ b	(insert $\epsilon$ )
aaaAb	$A  ightarrow \epsilon$
aaAb	A  ightarrow a $A$
aAb	A  ightarrow aA
Ab	A  ightarrow aA
AB	B  ightarrow b
5	S  ightarrow AB

### A naive top-down parser

- A very naive parsing algorithm:
  - Generate all possible parse trees until you get one that matches your input
  - To generate all parse trees:
    - 1. Start with the root of the parse tree (the start symbol of the grammar)
    - 2. Choose a non-terminal A at one leaf of the current parse tree
    - 3. Choose a production having that non-terminal as LHS, eg.,  $A \rightarrow X_1 X_2 \dots X_k$
    - 4. Expand the tree by making  $X_1, X_2, \ldots, X_k$ , the children of A.
    - 5. Repeat at step 2 until all leaves are terminals
    - $\mathbf{6}.$  Repeat the whole procedure by changing the productions chosen at step 3

( Note: the choice of the non-terminal in Step 2 is irrevelant for a context-free grammar)

This algorithm is very inefficient, does not always terminate, etc.

### Top-down parsing with backtracking

Modifications of the previous algorithm:

- 1. Depth-first development of the parse tree (corresponding to a left-most derivation)
- 2. Process the terminals in the RHS during the development of the tree, checking that they match the input
- 3. If they don't at some step, stop expansion and restart at the previous non-terminal with another production rules (backtracking)
- Depth-first can be implemented by storing the unprocessed symbols on a stack
- Because of the left-most derivation, the inputs can be processed from left to right

### Backtracking example

	Stack	Inputs	Action
	S	bcd	Try $S \rightarrow bab$
	bab	bcd	match <i>b</i>
S $ ightarrow$ bab	ab	cd	dead-end, backtrack
$S \rightarrow bA$	S	bcd	Try $S  ightarrow bA$
$A \rightarrow d$	bA	bcd	match <i>b</i>
	A	cd	Try $A  ightarrow d$
$A \rightarrow cA$	d	cd	dead-end, backtrack
	A	cd	Try $A  ightarrow cA$
	сA	cd	match <i>c</i>
w = bcd	A	d	Try $A  ightarrow d$
W - Ded	d	d	match <i>d</i>
			Success!

# Top-down parsing with backtracking

General algorithm (to match a word w): Create a stack with the start symbol X = POP()a = GETNEXTTOKEN()while (True) if (X is a nonterminal) Pick next rule to expand  $X \rightarrow Y_1 Y_2 \dots Y_k$ Push  $Y_k, Y_{k-1}, \ldots, Y_1$  on the stack X = POP()elseif (X == \$ and a == \$)Accept the input elseif (X == a)a = GETNEXTTOKEN()X = POP()else

Backtrack

- Ok for small grammars but still untractable and very slow for large grammars
- Worst-case exponential time in case of syntax error

### Another example

	Stack	Inputs	Action
	S	accbbadbc	Try $S \rightarrow aSbT$
$S \rightarrow aSbT$	aSbT	accbbadbc	match <i>a</i>
$S \rightarrow cT$	SbT	accbbadbc	Try $S  ightarrow aSbT$
$S \rightarrow d$	aSbTbT	accbbadbc	match <i>a</i>
0 / 1	SbTbT	ccbbadbc	Try $S  ightarrow cT$
T $ ightarrow$ $aT$	cTbTbT	ccbbadbc	match <i>c</i>
T  ightarrow bS	TbTbT	cbbadbc	Try $T  ightarrow c$
$T \rightarrow c$	cbTbT	cbbadbc	match <i>cb</i>
$I \rightarrow c$	TbT	badbc	Try $T  ightarrow bS$
	bSbT	badbc	match <i>b</i>
	SbT	adbc	Try $S \rightarrow aSbT$
	aSbT	adbc	match <i>a</i>
	С	С	match <i>c</i>
w = accbbadbc			Success!

# Predictive parsing

- Predictive parser:
  - In the previous example, the production rule to apply can be predicted based solely on the next input symbol and the current nonterminal
  - Much faster than backtracking but this trick works only for some specific grammars
- Grammars for which top-down predictive parsing is possible by looking at the next symbol are called *LL*(1) grammars:
  - L: left-to-right scan of the tokens
  - L: leftmost derivation
  - (1): One token of lookahead
- Predicted rules are stored in a parsing table *M*:
  - ► M[X, a] stores the rule to apply when the nonterminal X is on the stack and the next input terminal is a

### Example: parse table

$$S \rightarrow E\$$$
  

$$E \rightarrow int$$
  

$$E \rightarrow (E \text{ Op } E)$$
  

$$Op \rightarrow +$$
  

$$Op \rightarrow *$$

	int	(	)	+	*	\$
S	E\$	E\$				
E	int	(E Op E)				
Ор				+	*	

(Keith Schwarz)

### Example: successfull parsing

1. S $\rightarrow$ E\$
2. $E \rightarrow \texttt{int}$
3. E $\rightarrow$ (E Op E)
4. Op $\rightarrow$ +
5. Op → <b>-</b>

	int	(	)	+	*	\$
S	1	1				
Е	2	3				
Ор				4	5	

S	(int + (int * int))\$
E\$	(int + (int * int))\$
(E Op E) \$	(int + (int * int))\$
E Op E) \$	int + (int * int))\$
int Op E)\$	int + (int * int))\$
Op E)\$	+ (int * int))\$
+ E)\$	+ (int * int))\$
E)\$	(int * int))\$
(E Op E))\$	(int * int))\$
E Op E))\$	int * int))\$
int Op E))\$	int * int))\$
Op E))\$	* int))\$
* E))\$	* int))\$
E))\$	int))\$
int))\$	int))\$
))\$	))\$
)\$	)\$
\$	\$

(Keith Schwarz)

#### Example: erroneous parsing

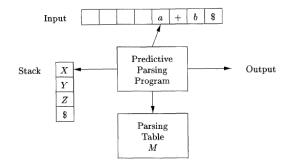
1. 
$$S \rightarrow E$$
\$  
2.  $E \rightarrow int$   
3.  $E \rightarrow (E \text{ Op } E)$   
4.  $Op \rightarrow +$   
5.  $Op \rightarrow -$ 

S	(int (int))\$
E\$	(int (int))\$
(E Op E) \$	(int (int))\$
E Op E) \$	int (int))\$
int Op E)\$	int (int))\$
Op E) \$	(int))\$

	int	(	)	+	*	\$
S	1	1				
Е	2	3				
Op				4	5	

(Keith Schwarz)

#### Table-driven predictive parser



(Dragonbook)

#### Table-driven predictive parser

```
Create a stack with the start symbol
X = POP()
a = GETNEXTTOKEN()
while (True)
     if (X is a nonterminal)
         if (M[X, a] == NULL)
              Frror
         elseif (M[X, a] = X \rightarrow Y_1 Y_2 \dots Y_k)
              Push Y_k, Y_{k-1}, \ldots, Y_1 on the stack
              X = POP()
     elseif (X == \$ and a == \$)
         Accept the input
     elseif (X == a)
         a = \text{GETNEXTTOKEN}()
         X = POP()
     else
         Frror
```

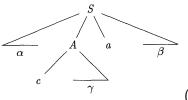
## LL(1) grammars and parsing

Three questions we need to address:

- How to build the table for a given grammar?
- How to know if a grammar is LL(1)?
- How to change a grammar to make it LL(1)?

#### Building the table

- It is useful to define three functions (with A a nonterminal and α any sequence of grammar symbols):
  - *Nullable*( $\alpha$ ) is true if  $\alpha \stackrel{*}{\Rightarrow} \epsilon$
  - *First*(α) returns the set of terminals c such that α ⇒ cγ for some (possibly empty) sequence γ of grammar symbols
  - ► Follow(A) returns the set of terminals a such that  $S \Rightarrow \alpha Aa\beta$ , where  $\alpha$  and  $\beta$  are (possibly empty) sequences of grammar symbols



 $(c \in First(A) \text{ and } a \in Follow(A))$ 

Building the table from First, Follow, and Nullable

To construct the table:

- Start with the empty table
- For each production  $A \rightarrow \alpha$ :
  - add  $A \rightarrow \alpha$  to M[A, a] for each terminal a in  $First(\alpha)$
  - If  $Nullable(\alpha)$ , add  $A \to \alpha$  to M[A, a] for each a in Follow(A)

First rule is obvious. Illustration of the second rule:

$$egin{array}{rcl} S & 
ightarrow Ab & Nullable(A) &= True \ A & 
ightarrow c & First(A) &= \{c\} & M[A,b] &= A 
ightarrow \epsilon \ A & 
ightarrow \epsilon & Follow(A) &= \{b\} \end{array}$$

# LL(1) grammars

#### Three situations:

- ► *M*[*A*, *a*] is empty: no production is appropriate. We can not parse the sentence and have to report a syntax error
- ▶ *M*[*A*, *a*] contains one entry: perfect !
- ► M[A, a] contains two entries: the grammar is not appropriate for predictive parsing (with one token lookahead)
- **Definition:** A grammar is LL(1) if its parsing table contains at most one entry in each cell or, equivalently, if for all production pairs  $A \rightarrow \alpha | \beta$ 
  - $First(\alpha) \cap First(\beta) = \emptyset$ ,
  - Nullable(α) and Nullable(β) are not both true,
  - if  $Nullable(\beta)$ , then  $First(\alpha) \cap Follow(A) = \emptyset$

• Example of a non *LL*(1) grammar:

$$\begin{array}{cccc} S & 
ightarrow & Ab \ A & 
ightarrow & b \ A & 
ightarrow & \epsilon \end{array}$$

### Computing Nullable

Algorithm to compute Nullable for all grammar symbols

Initialize Nullable to False. repeat for each production  $X \rightarrow Y_1 Y_2 \dots Y_k$ if  $Y_1 \dots Y_k$  are all nullable (or if k = 0) Nullable(X) = True until Nullable did not change in this iteration.

Algorithm to compute *Nullable* for any string  $\alpha = X_1 X_2 \dots X_k$ :

if  $(X_1 \dots X_k \text{ are all nullable})$   $Nullable(\alpha) = True$ else

 $Nullable(\alpha) = False$ 

## Computing First

Algorithm to compute First for all grammar symbols

Initialize *First* to empty sets. for each terminal Z *First*(Z) = {Z} repeat for each production  $X \rightarrow Y_1 Y_2 \dots Y_k$ for i = 1 to k if  $Y_1 \dots Y_{i-1}$  are all nullable (or i = 1) *First*(X) = *First*(X)  $\cup$  *First*(Y<sub>i</sub>) until *First* did not change in this iteration

until First did not change in this iteration.

Algorithm to compute *First* for any string  $\alpha = X_1 X_2 \dots X_k$ :

Initialize 
$$First(\alpha) = \emptyset$$
  
for  $i = 1$  to  $k$   
if  $X_1 \dots X_{i-1}$  are all nullable (or  $i = 1$ )  
 $First(\alpha) = First(\alpha) \cup First(X_i)$ 

## Computing Follow

To compute Follow for all nonterminal symbols

Initialize Follow to empty sets.

#### repeat

for each production  $X \rightarrow Y_1 Y_2 \dots Y_k$ for i = 1 to k, for j = i + 1 to kif  $Y_{i+1} \dots Y_k$  are all nullable (or i = k) Follow $(Y_i) = Follow(Y_i) \cup Follow(X)$ if  $Y_{i+1} \dots Y_{j-1}$  are all nullable (or i + 1 = j) Follow $(Y_i) = Follow(Y_i) \cup First(Y_j)$ 

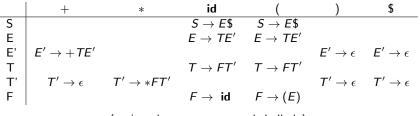
until Follow did not change in this iteration.

#### Example

Compute the parsing table for the following grammar:

## Example

Nonterminals	Nullable	First	Follow	
S	False	$\{(, id, num \}$	Ø	
E	False	$\{(, id, num \}$	{), <b>\$</b> }	
E'	True	$\{+, -\}$	{), <b>\$</b> }	
Т	False	$\{(, id, num \}$	$\{), +, -, \$\}$	
T'	True	$\{*, /\}$	$\{), +, -, \$\}$	
F	False	$\{(, id, num \}$	$\{), *, /, +, -, \$\}$	



(-,/, and num are treated similarly)

## LL(1) parsing summary so far

Construction of a LL(1) parser from a CFG grammar

- Eliminate ambiguity
- Add an extra start production S' o S\$ to the grammar
- Calculate *First* for every production and *Follow* for every nonterminal
- Calculate the parsing table
- Check that the grammar is *LL*(1)

Next course:

- Transformations of a grammar to make it LL(1)
- Recursive implementation of the predictive parser
- Bottom-up parsing techniques